An Improved C-Band Ocean Surface Emissivity Model at Hurricane-Force Wind Speeds Over a Wide Range of Earth Incidence Angles

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Abstract—An improved microwave radiometric ocean surface emissivity model has been developed to support forward radiative transfer modeling of brightness temperature and geophysical retrieval algorithms for the next-generation airborne Hurricane Imaging Radiometer instrument. This physically based C-band emissivity model extends current model capabilities to hurricane-force wind speeds over a wide range of incidence angles. It was primarily developed using brightness temperature observations during hurricanes with coincident high-quality surface-truth wind speeds, which were obtained using the airborne Stepped-Frequency Microwave Radiometer. Also, other ocean emissivity models available through the published literature and the spaceborne WindSat radiometer measurements were used.

Index Terms—Hurricane Imaging Radiometer (HIRAD), hurricane winds, ocean surface emissivity, radiometry, Stepped-Frequency Microwave Radiometer (SFMR).

I. INTRODUCTION

AIRBORNE hurricane surveillance provides crucial real-time measurements that are vital to hurricane forecast warnings issued by the National Oceanic and Atmospheric Administration (NOAA) National Hurricane Center (NHC). NOAA and the U.S. Air Force (USAF) Reserve 53rd Weather Reconnaissance Squadron fly specially equipped “Hurricane Hunter” aircraft into storms of the Caribbean Sea and the Atlantic Ocean that threaten the continental U.S. Data collected by in situ and remote sensing instruments are delivered in real time to the NHC to help forecasters predict the intensity of the hurricane and its track. Airborne measurements include the hurricane eye location, the central pressure, and the peak surface wind speed. Of these, the maximum sustained (1-min average) surface wind speed at the 10-m level is of greatest importance because this is the determining factor in the Saffir–Simpson hurricane scale commonly known as the hurricane category. For the past two decades, the airborne Stepped-Frequency Microwave Radiometer (SFMR) has provided real-time measurements of surface wind speed and rain rates in hurricanes [1]. These measurements are crucial because SFMR is the only remote sensor that is capable of providing continuous measurements of surface wind speeds up to and including Category-5 (CAT5) hurricane conditions. Furthermore, since 2006, operational SFMR sensors have been installed on both NOAA WP-3D and USAF WC-130J aircraft.

The Hurricane Imaging Radiometer (HIRAD) is the next-generation version of SFMR, which is developed by the National Aeronautics and Space Administration Marshall Space Flight Center, the NOAA Hurricane Research Division (HRD), the University of Michigan, and the Central Florida Remote Sensing Laboratory (CFRSL). HIRAD is a hybrid design that is both a multifrequency radiometer, similar to SFMR, and a Fourier synthesis imager, similar to the Lightweight Rain Radiometer [2]. It uses synthetic thinned-array interferometric radiometry to synthesize C-band (4–6.6-GHz) ocean brightness temperature ($T_b$) pixels cross track and real-aperture pushbroom imaging along track [3] for retrievals of hurricane surface winds and rain rates over a swath width of approximately three times the aircraft altitude. Extending the nadir-viewing SFMR wind speed retrieval capabilities to HIRAD requires the development of a more general ocean surface emissivity model, which is the subject of this letter.

II. OCEAN EMISSIVITY MODEL FORMULATION

For HIRAD, the retrieval of hurricane wind speed requires an ocean emissivity model that must accommodate the full range of Earth incidence angles ($EIA$) from nadir to $>60^\circ$ and ocean wind speeds from 10 m/s to CAT5 winds under atmospheric boundary layer stability conditions from neutral to slightly unstable that are typical of most hurricanes. There are many ocean emissivity models available, but unfortunately, none fully satisfies these stringent HIRAD requirements. Because of the limited availability of off-nadir C-band $T_b$ observations in hurricanes and the difficulty of performing new
measurements with associated surface truth, we have developed a hybrid physically based/empirically tuned model, which provides the flexibility of extrapolating ocean emissivity to other regimes where measurements are possible but have not yet been observed.

A. Existing Ocean Emissivity Models

There are three ocean emissivity models, which are applicable to HIRAD. First, the NOAA SFMR emissivity model by Uhlhorn et al. [1] is the only model that is capable of estimating ocean emissivity over the full range of wind speeds from 10 to > 70 m/s. This empirical statistical regression model is based upon SFMR C-band \( T_b \) measurements in hurricanes that are collocated with 10-m ocean surface wind speed measurements derived from GPS dropwindsones; however, because this algorithm applies only at nadir, its utility to HIRAD is limited. Second, the model by Stogryn [4] is a physically based approach, with empirical coefficients based on radiometric measurements of foam-covered sea surfaces, which calculates the ocean emissivity for the HIRAD frequencies and EIA range. Unfortunately, this model exhibits unrealistic emissivity saturation at wind speeds > 45 m/s; therefore, significant corrections are required. Third, the emissivity model by Wentz and Meissner [5] has been developed for conical scanning satellite radiometers, but it is limited to a narrow range of EIA’s (49°–57°) and for wind speeds < 20 m/s. Thus, because no single model is fully satisfactory, all three ocean emissivity models are used in the development of the new CFRSL HIRAD emissivity model [6].

B. CFRSL Ocean Emissivity Model

This model uses the formulation of Stogryn with modified model coefficients that are tuned to Uhlhorn and Wentz ocean emissivities in their range of applicability and new off-nadir hurricane \( T_b \) measurements for SFMR and WindSat. Where empirical data do not exist, the emissivity is constrained to vary smoothly in a monotonic manner and without an inflection point in the first derivative with respect to model parameters (wind speed, EIA, and frequency). Furthermore, to extrapolate model parameters beyond the range of observations, the CFRSL emissivities are constrained to asymptotically approach physically realizable limits. All model coefficients are derived in an iterative manner to provide a weighted least mean squares fit to empirical realizable limits. All model coefficients are derived in an iterative manner to provide a weighted least mean squares fit to

\[
\begin{align*}
\epsilon_{\text{ocean}} &= FF \times \epsilon_{\text{foam}} + (1 - FF) \times \epsilon_{\text{rough}} \\
\epsilon_{\text{foam}} &= Q(freq) \times f(U_{10}, \text{EIA}) \\
\epsilon_{\text{rough}} &= \epsilon_{\text{smooth}} + \Delta \epsilon_{\text{excess}} \\
\Delta \epsilon_{\text{excess}} &= g(U_{10}, \text{EIA}) \times \sqrt{\frac{\text{freq}}{\text{SST}}} \\
\end{align*}
\]

where \( \epsilon_{\text{foam}} \) is the fractional area coverage by foam. The foam emissivity is modeled as

\[
Q(freq) = 0.036659 \times freq + 0.57767
\]

where \( freq \) has units of gigahertz.

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Next, the dependence of $FF$ on wind speed was derived using the Uhlhorn emissivity model over the dynamic range of 0–70 m/s. In this calculation, Stogryn’s $\varepsilon_{\text{rough}}$ was used; however, since the function $f(U_{10}, \text{EIA} = 0)$ in (4) was allowed to change, the $FF$ was also calculated iteratively

$$FF = \frac{\langle \varepsilon_{\text{SFMR}} \rangle_{\text{freq}} - \langle \varepsilon_{\text{rough}} \rangle_{\text{freq}}}{\langle \varepsilon_{\text{foam}} \rangle_{\text{freq}} - \langle \varepsilon_{\text{rough}} \rangle_{\text{freq}}} \tag{6}$$

where “\langle \rangle” denotes average values. At wind speeds > 70 m/s, $FF$ was modeled to asymptotically approach 100%, as shown in Fig. 1. Also shown are independent measurements from the Coupled Boundary Layer Air–Sea Transfer (CBLAST) experiment [7] of foam fractional coverage ($FFC$), in the North Atlantic from Callaghan et al. [8], Bondur and Skarkov [9], and Monahan and Woolf [10], which compare well with our model. The Melville/Kleiss CBLAST and GOTEK foam whitecap coverage ($FWC$) were added to Fig. 1 for completeness and to show the difference between $FWC$ and $FFC$, where $FFC$ is the main interest because it represents the total foam coverage (whitecaps and streaks).

2) Wind Speed and EIA Coefficient Tuning: The HIRAD geometry requires an emissivity model that is applicable from nadir to $> 60^\circ$ over the full range of wind speeds (0–70 m/s). Based upon the findings of Reul and Chapron [11], we model the emissivity of foam in (2) as a function of $U_{10}$ and EIA. The functional form of this dependence was developed empirically using SFMR (airborne) and WindSat (satellite) measurements in several hurricanes with near-simultaneous aircraft underflights providing “surface truth.” Radiometric measurements at off-nadir angles were collected at wind speeds greater than 20 m/s, where foam has an appreciable contribution to the total ocean emission.

a) SFMR measurements: This data set comprised brightness temperatures from SFMR flights during the 2003–2005 hurricane seasons (Table I). It included measurements at high wind speeds and off-nadir incidence angles up to $35^\circ$ for H-pol and vertical polarization (V-pol) that were analyzed to extract the ocean surface emissivity from SFMR brightness temperatures. First, the data were filtered to extract off-nadir measurements during steady aircraft turns, which resulted in a small data set with reduced dynamic range of available wind speeds. This occurred because turns were not performed in the eye wall region (maximum winds) due to safety concerns. Next, the data were examined for radio-frequency interference (RFI) detection, and contaminated SFMR measurements were removed from the data set. Because of onboard C-band radars, RFI was experienced on one or more channels approximately 15%–25% of the time. Fortunately, the RFI was relatively easy to detect by relative comparison among SFMR channels using a $T_b$ threshold.

The next step involved “atmospheric clearing” to remove the atmospheric component of SFMR $T_b$ before estimation of the ocean surface emissivity. For this purpose, radiative transfer calculations were performed using a typical hurricane atmosphere by Frank [12]. Furthermore, the effects of rain (emission and attenuation) were removed using the approach of Uhlhorn et al. [1], [13]. Data sets were carefully selected to minimize regions with heavy rain, but typically, rain atmospheric clearing was required. This involved estimating the rain rate along the propagation path using SFMR rain retrievals during level flight before and after the turns. For atmospheric clearing, the rain was assumed to be homogeneous with a 100% antenna beam fill. This is considered to be valid because the SFMR operated at low altitudes (< 2.5 km) and at low bank angles (< $35^\circ$), which resulted in the line of sight being displaced by < 1.75 km from nadir. Atmospheric clearing typically yielded $T_b$ adjustments of < 5 K [6].

The final data reduction step involved an antenna pattern correction to remove $T_b$ biases caused by the broad SFMR antenna beamwidth ($15^\circ–28^\circ$). In this procedure, we first calculated the antenna temperature as a weighted average (convolution) of the antenna gain pattern with the Fresnel smooth surface $T_b$, as a function of $EIA$. Next, the differential between this antenna pattern-weighted $T_b$ and the Fresnel brightness was calculated versus $EIA$. Finally, this was subtracted from the SFMR measurement to yield the corrected $T_b$. Typically, this process resulted $T_b$ biases < 4 K (depending on the aircraft roll angle) and yielded an improved estimate of the true brightness temperature at the antenna boresight $EIA$ [6].

b) Satellite measurements: For high $EIA$ ($49^\circ–57^\circ$), the surface emissivity model by Wentz and Meissner [5] was used to estimate the total ocean emissivity versus wind speed. Wentz and Meissner’s results were based upon over one decade of Special Sensor Microwave/Imager and Tropical Rainfall

**Table I**

<table>
<thead>
<tr>
<th>Hurricane</th>
<th>Year</th>
<th>max 1-min sustained wind speed</th>
<th>Number of flights</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fabian</td>
<td>2003</td>
<td>120 kt (60 m/s)</td>
<td>3</td>
</tr>
<tr>
<td>Frances</td>
<td>2004</td>
<td>115 kt (58 m/s)</td>
<td>6</td>
</tr>
<tr>
<td>Katrina</td>
<td>2005</td>
<td>150 kt (75 m/s)</td>
<td>4</td>
</tr>
<tr>
<td>Ophelia</td>
<td>2005</td>
<td>65 kt (34 m/s)</td>
<td>4</td>
</tr>
<tr>
<td>Rita</td>
<td>2005</td>
<td>155 kt (78 m/s)</td>
<td>5</td>
</tr>
</tbody>
</table>

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Measuring Mission Microwave Imager $T_b$ comparisons with in situ wind speed measurements on buoys, which were extrapolated to the HIRAD C-band frequencies. The buoy data set only extended to $\sim$20 m/s; therefore, hurricane observations from the WindSat polarimetric radiometer were used for higher wind speeds.

An analysis of WindSat C-band (6.8 GHz) V- and H-pol $T_b$ in hurricanes by Ruf et al. [14] was used to estimate the total ocean emissivity at high wind speeds and $EIA_s (49^\circ–55^\circ)$. This study involved satellite radiometer measurements obtained during 2005 hurricanes (Dennis, Rita, and Katrina) and associated high-quality surface wind fields derived from NOAA HRD aircraft underflights with SFMR. Results showed a well-behaved and monotonic increase in the C-band ocean emissivity with surface wind speed provided using NOAA’s H’Wind analysis procedure (see [14, Table 1 and Fig. 5]). These data were extrapolated to HIRAD’s C-band frequencies (4–6.6 GHz) and were then used subjectively as points of reference at higher $EIA$ ($>45^\circ$) in a weighted least mean squares sense to derive $f(U_{10}, EIA)$ in (2).

c) Wind speed modeling: Because of the distinct contributions by rough water and foam in (1), modeling of the ocean surface emissivity was broken into two parts: wind speeds $U_{10} \leq 20$ m/s and higher wind speeds. In both cases, measurements from SFMR and satellites were used to estimate our model coefficients using regression analysis, and special care was taken to assure a smooth transition with wind speed.

For wind speeds $5 \leq U_{10} \leq 20$ m/s, the rough-water emissivity term dominates, and both sets (aircraft and satellite) of total ocean emissivities were used to derive $g(U_{10}, EIA)$ in (4). Ocean emissivity values derived from SFMR measurements were binned and averaged with respect to $U_{10}$ (5-m/s bins) and $EIA$ from nadir to $35^\circ$ ($2^\circ$ bins). For high $EIA (49^\circ–57^\circ)$, the surface emissivity model by Wentz and Meissner [5] was extrapolated to SFMR frequencies and used to provide the ocean emissivity versus wind speed at higher $EIA$. While the Wentz and Meissner model has not been validated versus wind speed below 10.6 GHz, we feel that uncertainties due to extrapolation to C-band are not dominant over the wind speed range used.

The dependence of emissivity on $EIA$ was assumed to be
monotonic from nadir for both polarizations (increasing for V-pol but decreasing for H-pol). For the regression analysis, each binned data point was given an independent weight based on the number of points in that bin and the subjective confidence of these measurements. For V-pol, the number of SFMR observations is significantly less, and the resulting regression fit for the CFRSL emissivity model has much higher residuals. This was particularly true for SFMR measurements between 20° and 30°, which were of lesser quality because of possible errors in the atmospheric clearing for rain effects.

For higher wind speeds ($U_{10} > 20$ m/s), foam becomes the dominant contributor to ocean surface emissivity; and SFMR and WindSat hurricane observations were used to estimate the foam emissivity dependence on wind speed and $E_{IA}$. The $f(U_{10}, E_{IA})$ in (2) was derived from a regression analysis using only SFMR data (WindSat data were used subjectively as constraints), and results for H-pol are shown in Fig. 2. Because of spatial averaging over the large antenna footprint (40 km × 60 km), we believe that the WindSat emissivities [14] for both V- and H-pols are progressively underestimated with increasing wind speed.

### III. Results

The results shown in Fig. 3 show the total ocean emissivity measurements in the range $5 \leq U_{10} \leq 20$ m/s, where emissivities based upon experimental observations (symbols) were from SFMR (nadir–35°) and Wentz [49°–57°]. CFRSL model results (solid lines) are in excellent agreement with these total ocean emissivity values for both polarizations. As discussed previously, the V-pol SFMR total emissivity values have greater deviations from our model between 20° and 30°, but we believe that our model’s monotonic dependence on $E_{IA}$ is more consistent with electromagnetic theory than are the SFMR measurements during aircraft banked turns.

The results shown in Fig. 4 compare the CFRSL model with surface emissivity values, derived from SFMR and WindSat, over the wind speed range of 20–45 m/s. For H-pol (left panel), the model (solid lines) exhibits excellent agreement with the SFMR, but the agreement with WindSat is slightly degraded as the wind speed increases. As discussed earlier, we believe that the WindSat emissivities are too low because of spatial averaging over the large antenna footprint. On the other hand, the V-pol comparisons of the CFRSL model with the SFMR and WindSat data exhibit relatively larger differences. As discussed before, we attribute this to the lesser quality of the SFMR and WindSat data.

Finally, two independent SFMR measurements of total ocean emissivity are available from NOAA HRD during the 2008 hurricane season (hurricanes Dolly and Gustav).

In these experiments, the NOAA WP3 aircraft flew consecutive circles at 30° and 45° banks in clear (rain-free) regions with surface wind speeds of 15 m/s (see the Fig. 3 left panel) and 35 m/s (see the Fig. 4 left panel) [15]. Since these measurements were not used in the CFRSL model development, they are shown in Figs. 3 and 4 as points of independent comparison. There is excellent agreement with the CFRSL model for these two high-quality off-nadir emissivity measurements.

### IV. Summary and Conclusion

This letter has presented a new microwave (C-band: 4–6.6 GHz) ocean surface emissivity model that has been developed for the airborne HIRAD instrument for hurricane remote sensing applications. This model extends the capability of current ocean emissivity models to a wider range of $E_{1As}$ (0°–60°), higher wind speeds (0–70 m/s), and for both H- and V-pols. This model has been tuned using available airborne (SFMR) hurricane measurements, an extrapolated spaceborne radiometer emissivity model (Wentz and Meissness [5]), and WindSat measurements in hurricane conditions. The model exhibits a good fit with low residuals over a wide range of $E_{1As}$ and wind speeds. Also, the derived relationship for hurricane sea foam parameters with respect to wind speed agrees well with independent FFC observations and foam emissivity measurements in the C-band frequency range. Future improvements are expected once the HIRAD instrument flies in hurricanes during the 2010 season.

### References